

# Problem set 1

November 11, 2011

## Exercise 1 (Romer, 1.2)

Suppose that the growth rate of some variable,  $X$ , is constant and equal to  $a > 0$  from time  $t = 0$  to  $t = t_1$ ; drops to 0 at time  $t_1$ ; rises gradually from 0 to  $a$  from time  $t_1$  to  $t_2$ ; and is constant and equal to  $a$  after  $t_2$ .

1. Sketch a graph of the growth rate of  $X$  as a function of time.
2. Sketch a graph of  $\log X$  as a function of time

## Exercise 2 (Romer, 1.5)

Consider Solow model with technological and population growth (with growth rates  $g$  and  $n$  respectively) and depreciation rate  $\delta$  as we derived it in the class. Suppose  $F(K, AL) = K^\alpha(AL)^{1-\alpha}$ .

1. Find expressions for  $k^*$ ,  $y^*$  and  $c^*$  as function of the parameters of the model  $s, n, g, \delta$  and  $\alpha$ .
2. What is the golden-rule value of  $k$ ?
3. What saving rate  $s^*$  is needed to yield the golden rule capital stock?

## Exercise 3

Consider Solow model with population and technological growth ( $n, g$ ). Also, we know that  $\delta K_{t+1} = sF(K_t, A_t L_t) + (1 - \delta)K_t$ . In the class we have used the continuous time calculus to derive  $\dot{k} = sf(k) - (n + g + \delta)k$ .

Working with the discrete variables, show that

$$(1 + g + n)(k_{t+1} - k_t) = sf(k) - (n + g + \delta)k_t.$$

## Exercise 4

In the framework of the dynamic model we have derived in the class, consider a simple modification by adding the government. The demand for output is hence given by private consumption and government expenditures:  $Y^D = C + G$ .

1. describe the intertemporal government budget constraint
2. analyze the effects of a *permanent* and a *temporary* increase of government spending.

(*hint*: How strong is the wealth effect in either case?)